

# SUSY: From the Basics to Collider Phenomenology

*Sven Heinemeyer, IFCA (Santander)*

Louvain, 05/2007

- 1.** Introduction to SUSY
- 2.** SUSY Lagrangians and the MSSM
- 3.** “Simplified versions” and special sectors
- 4.** SUSY Phenomenology

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# **SUSY lectures (II): SUSY Lagrangians and the MSSM**

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- 1.** Supersymmetric Lagrangians
- 2.** Soft SUSY-breaking
- 3.** The Minimal Supersymmetric Standard Model (MSSM)
- 4.** Properties of SUSY Theories

## 1. Supersymmetric Lagrangians

Aim: construct an action that is invariant under SUSY transformations:

$$\delta \int d^4x \mathcal{L}(x) = 0$$

Satisfied if  $\mathcal{L} \rightarrow \mathcal{L} + \text{total derivative}$

*F* and *D* terms (the terms with the largest number of  $\theta$  and  $\bar{\theta}$  factors) of chiral and vector superfields transform into a total derivative under SUSY transformations

⇒ Use *F*-terms (LH $\chi$ SF, RH $\chi$ SF) and *D*-terms (Vector SF) to construct an invariant action:

$$S = \int d^4x \left( \int d^2\theta \mathcal{L}_F + \int d^2\theta d^2\bar{\theta} \mathcal{L}_D \right)$$

If  $\Phi$  is a LH $\chi$ SF  $\Rightarrow$   $\Phi^n$  is also a LH $\chi$ SF (since  $\bar{D}_{\dot{\alpha}}\Phi^n = 0$  for  $\bar{D}_{\dot{\alpha}}\Phi = 0$ )

⇒ products of chiral superfields are chiral superfields, products of vector superfields are vector superfields

*F*-term Lagrangian:

$$\mathcal{L}_F = \int d^2\theta \sum_{ijk} \left( a_i \Phi_i + \frac{1}{2} m_{ij} \Phi_i \Phi_j + \frac{1}{3} \lambda_{ijk} \Phi_i \Phi_j \Phi_k \right) + \text{h.c.}$$

Terms of higher order in  $\Phi_i$  lead to non-renormalizable Lagrangians

⇒ *F*-term Lagrangian contains mass terms, scalar–fermion interactions  
(→ superpotential), but no kinetic terms

*D*-term Lagrangian:

$$\mathcal{L}_D = \int d^2\theta d^2\bar{\theta} V$$

⇒ *D*-term Lagrangian contains kinetic terms

## Example: the Wess–Zumino Lagrangian

Construction of Lagrangian from chiral superfields  $\Phi_i$

⇒  $\Phi_i, \Phi_i\Phi_j, \Phi_i\Phi_j\Phi_k$

$\Phi_i^\dagger\Phi_i$ : vector superfield,  $(\Phi_i^\dagger\Phi_i)^\dagger = \Phi_i^\dagger\Phi_i$

$$[\Phi_i^\dagger\Phi_i]_{\theta\bar{\theta}\bar{\theta}\bar{\theta}} = F^\dagger F + (\partial_\mu\varphi^*)(\partial^\mu\varphi) + \frac{i}{2}(\psi\sigma^\mu\partial_\mu\bar{\psi} - \partial_\mu\psi\sigma^\mu\bar{\psi}) + \partial_\mu(\dots)$$

Auxiliary field  $F$  can be eliminated via equations of motion

→ Construction of a (simplified) Wess–Zumino Lagrangian

## Example: the Wess–Zumino Lagrangian

Construction of Lagrangian from chiral superfields  $\Phi_i$

$$\Rightarrow \Phi_i, \Phi_i\Phi_j, \Phi_i\Phi_j\Phi_k$$

$\Phi_i^\dagger\Phi_i$ : vector superfield,  $(\Phi_i^\dagger\Phi_i)^\dagger = \Phi_i^\dagger\Phi_i$

$$[\Phi_i^\dagger\Phi_i]_{\theta\bar{\theta}\bar{\theta}\bar{\theta}} = F^\dagger F + (\partial_\mu\varphi^*)(\partial^\mu\varphi) + \frac{i}{2}(\psi\sigma^\mu\partial_\mu\bar{\psi} - \partial_\mu\psi\sigma^\mu\bar{\psi}) + \partial_\mu(\dots)$$

Auxiliary field  $F$  can be eliminated via equations of motion

Including all indices:

$$\begin{aligned} \Rightarrow \mathcal{L}_D = & \frac{i}{2}(\psi_i\sigma^\mu\partial_\mu\bar{\psi}_i - (\partial_\mu\psi_i)\sigma^\mu\bar{\psi}_i) - \frac{1}{2}m_{ij}(\psi_i\psi_j + \bar{\psi}_i\bar{\psi}_j) \\ & + (\partial_\mu\varphi_i^*)(\partial^\mu\varphi_i) - \sum_i \left| a_i + \frac{1}{2}m_{ij}\varphi_j + \frac{1}{3}\lambda_{ijk}\varphi_j\varphi_k \right|^2 \\ & - \lambda_{ijk}\varphi_i\psi_j\psi_k - \lambda_{ijk}^\dagger\varphi_i^*\bar{\psi}_j\bar{\psi}_k \end{aligned}$$

Auxiliary fields are eliminated via equations of motions:

$$\begin{aligned} \text{abelian : } F &= m\varphi^* + g\varphi^{*2} \\ \text{non-abelian, gauge group } G : D^G &= \dots \sum_a g_G (\varphi_i^\dagger (T_G)^a \varphi_i) \\ &\quad (\text{internal indices of } T_G, \varphi_i \text{ suppressed}) \end{aligned}$$

$$\Rightarrow \mathcal{L}_D = F F^* + \frac{1}{2} \sum_G D^G (D^G)^\dagger + \dots$$

Lagrangian for scalar fields  $\varphi_i$  and spinor fields  $\psi_i$  with the **same mass**  $m_{ii}$  contains couplings of type  $h f \bar{f}$  and  $\tilde{h} \tilde{f} \bar{f}$  with the **same strength**

⇒ SUSY implies relations between masses and couplings

$\mathcal{L}$  can be rewritten as kinetic part + contribution of superpotential  $\mathcal{V}$  :

$$\mathcal{V}(\varphi_i) = a_i \varphi_i + \frac{1}{2} m_{ij} \varphi_i \varphi_j + \frac{1}{3} \lambda_{ijk} \varphi_i \varphi_j \varphi_k$$

$$\Rightarrow \mathcal{L} = \frac{i}{2} (\psi_i \sigma^\mu \partial_\mu \bar{\psi}_i - (\partial_\mu \psi_i) \sigma^\mu \bar{\psi}_i) + (\partial_\mu \varphi_i^*) (\partial^\mu \varphi_i)$$
$$- \sum_i \left| \frac{\partial \mathcal{V}}{\partial \varphi_i} \right|^2 - \frac{1}{2} \frac{\partial^2 \mathcal{V}}{\partial \varphi_i \partial \varphi_j} \psi_i \psi_j - \frac{1}{2} \frac{\partial^2 \mathcal{V}^*}{\partial \varphi_i^* \partial \varphi_j^*} \bar{\psi}_i \bar{\psi}_j$$

$\mathcal{V}$  determines all interactions and mass terms

Without proof:

characteristics of  $\mathcal{V}$  = characteristics of  $\mathcal{L}$

Special case  $a_i = 0$ : Wess–Zumino model

## 2. Soft SUSY-breaking

Exact SUSY:  $m_f = m_{\tilde{f}}, \dots$

⇒ in a realistic model: **SUSY must be broken**

Only satisfactory way for model of SUSY breaking:

spontaneous SUSY breaking

Specific SUSY-breaking schemes (see below) in general yield effective Lagrangian at low energies, which is supersymmetric except for explicit **soft SUSY-breaking terms**

Soft SUSY-breaking terms: do not alter dimensionless couplings

(i.e. dimension of coupling constants of soft SUSY-breaking terms  $> 0$ )  
otherwise: **re-introduction of the hierarchy problem**

⇒ **no quadratic divergences** (in all orders of perturbation theory)

scale of SUSY-breaking terms:  $M_{\text{SUSY}} \lesssim 1 \text{ TeV}$

## Classification of possible soft breaking terms:

[*L. Girardello, M. Grisaru '82*]

- scalar mass terms:  $m_{\phi_i}^2 |\phi_i|^2$
- trilinear scalar interactions:  $A_{ijk}\phi_i\phi_j\phi_k + \text{h.c.}$
- gaugino mass terms:  $\frac{1}{2}m\bar{\lambda}\lambda$
- bilinear terms:  $B_{ij}\phi_i\phi_j + \text{h.c.}$
- linear terms:  $C_i\phi_i$

⇒ relations between dimensionless couplings unchanged

no additional mass terms for chiral fermions

## A. Unconstrained models (MSSM):

agnostic about how SUSY breaking is achieved  
no particular SUSY breaking mechanism assumed, parameterization of possible soft SUSY-breaking terms

⇒ relations between dimensionless couplings unchanged  
no quadratic divergences

most general case:

⇒ 105 new parameters: masses, mixing angles, phases

Good phenomenological description for universal breaking terms

## B. Constrained models (mSUGRA, . . .):

assumption on the scenario that achieves spontaneous SUSY breaking

⇒ prediction for soft SUSY-breaking terms  
in terms of small set of parameters

Experimental determination of SUSY parameters

⇒ Patterns of SUSY breaking

Problems can be overcome if SUSY breaking happens in a ‘hidden sector’, i.e. by fields which have only very small couplings to ordinary matter

SUSY breaking in the hidden sector:

- tree-level (like  $F$ - and  $D$ -term breaking)
- dynamical breaking (similar to chiral symmetry breaking in QCD), . . .

SUSY-breaking terms in the MSSM arise radiatively via interaction that communicates SUSY breaking rather than through tree-level couplings to SUSY breaking v.e.v.s

⇒ phenomenology depends mainly on mechanism for communicating SUSY breaking rather than on SUSY-breaking mechanism itself

If mediating interactions are  $\approx$  flavor-diagonal

⇒ universal soft-breaking terms

“Hidden sector” : → Visible sector:  
SUSY breaking                                   MSSM

“Gravity-mediated”: mSUGRA

“Gauge-mediated”: GMSB

“Anomaly-mediated”: AMSB

“Gaugino-mediated”

...

SUGRA: mediating interactions are gravitational

GMSB: mediating interactions are ordinary electroweak and QCD  
gauge interactions

AMSB, Gaugino-mediation: SUSY breaking happens on a different brane  
in a higher-dimensional theory

(more details later)

### 3. The Minimal Supersymmetric Standard Model (MSSM)

MSSM: superpartners for SM fields

SM matter fermions have different quantum numbers than  
SM gauge bosons

⇒ need to be placed in different superfields

⇒ no SM fermion is a gaugino

no Higgs is a sfermion (e.g. scalar neutrino)

agnostic about how SUSY breaking is achieved

no particular SUSY breaking mechanism assumed

parameterization of possible soft SUSY-breaking terms

⇒ most general case: 105 new parameters: masses, mixing angles, phases

## 1. Fermions, sfermions:

left-handed chiral superfields give SM fermions/sfermions  
( $\Rightarrow$  the conjugates of right-handed ones appear)

$LH\chi SF \ Q$ : quark, squark SU(2) doublets

$LH\chi SF \ U$ : up-type quark, squark singlets

$LH\chi SF \ D$ : down-type quark, squark singlets

$LH\chi SF \ L$ : lepton, slepton SU(2) doublets

$LH\chi SF \ E$ : lepton, slepton singlets

$\Rightarrow$  one generation of SM fermions and their superpartners described by five  $LH\chi SFs$

## 2. Gauge bosons, gauginos:

## Vector superfields:

- gluons  $g$  and gluinos  $\tilde{g}$
  - W bosons  $W^\pm, W^0$  and winos  $\tilde{W}^\pm, \tilde{W}^0$
  - B boson  $B^0$  and bino  $\tilde{B}^0$

### 3. Higgs bosons, higgsinos:

LH $\chi$ SF

In MSSM: two Higgs doublets needed  $\Rightarrow$  two LH $\chi$ SFs

Comparison with SM case:

$$\mathcal{L}_{\text{SM}} = \underbrace{m_d \bar{Q}_L H d_R}_{\text{d-quark mass}} + \underbrace{m_u \bar{Q}_L \tilde{H} u_R}_{\text{u-quark mass}}$$

$$Q_L = \begin{pmatrix} u \\ d \end{pmatrix}_L, \quad \tilde{H} = i\sigma_2 H^\dagger, \quad H \rightarrow \begin{pmatrix} 0 \\ v \end{pmatrix}, \quad \tilde{H} \rightarrow \begin{pmatrix} v \\ 0 \end{pmatrix}$$

In SUSY: term  $\bar{Q}_L H^\dagger$  not allowed

Superpotential is holomorphic function of chiral superfields, i.e. depends only on  $\varphi_i$ , not on  $\varphi_i^*$

No soft SUSY-breaking terms allowed for chiral fermions

⇒  $H_d$  and  $H_u$  needed to give masses to down- and up-type fermions

Furthermore: two doublets also needed for cancellation of anomalies, quadratic divergences

## Chiral supermultiplets of the MSSM:

		spin 0	spin $\frac{1}{2}$	$(\text{SU}(3)_c, \text{SU}(2), \text{U}(1)_Y)$
squarks and quarks	$Q$	$(\tilde{u}_L, \tilde{d}_L)$	$(u_L, d_L)$	$(3, 2, \frac{1}{6})$
	$U$	$\tilde{u}_R^*$	$u_R^+$	$(\bar{3}, 1, -\frac{2}{3})$
	$D$	$\tilde{d}_R^*$	$d_R^+$	$(\bar{3}, 1, \frac{1}{3})$
sleptons and leptons	$L$	$(\tilde{\nu}, \tilde{e}_L)$	$(\nu, e_L)$	$(1, 2, -\frac{1}{2})$
	$E$	$\tilde{e}_R^*$	$e_R^+$	$(1, 1, 1)$
higgs and higgsinos	$H_u$	$(h_u^+, h_u^0)$	$(\tilde{h}_u^+, \tilde{h}_u^0)$	$(1, 2, \frac{1}{2})$
	$H_d$	$(h_d^0, h_d^-)$	$(\tilde{h}_d^0, \tilde{h}_d^-)$	$(1, 2, -\frac{1}{2})$

## Vector supermultiplets:

	spin $\frac{1}{2}$	spin 1	( $SU(3)_c$ , $SU(2)$ , $U(1)_Y$ )
gluinos and gluons	$\tilde{g}$	$g$	(8, 1, 0)
winos and $W$ -bosons	$\widetilde{W}^\pm, \widetilde{W}^0$	$W^\pm, W^0$	(1, 3, 0)
bino and $B$ -boson	$\widetilde{B}$	$B$	(1, 1, 0)

⇒ MSSM has further symmetry: “R-parity”

all SM-particles and Higgs bosons: even R-parity,  $P_R = +1$

all superpartners: odd R-parity,  $P_R = -1$

⇒ SUSY particles appear only in pairs

⇒ lightest SUSY particle (LSP) is stable

## Soft breaking terms:

$$\begin{aligned}\mathcal{L}_{\text{soft}} = & -\frac{1}{2} \left( \textcolor{teal}{M}_1 \tilde{B} \tilde{B} + \textcolor{teal}{M}_2 \tilde{W} \tilde{W} + \textcolor{teal}{M}_3 \tilde{g} \tilde{g} \right) + \text{h.c.} \quad (1) \\ & - (\textcolor{teal}{m}_{H_u}^2 + |\mu|^2) H_u^+ H_u - (\textcolor{teal}{m}_{H_d}^2 + |\mu|^2) H_d^+ H_d - (\textcolor{teal}{b} H_u H_d + \text{h.c.}) \\ & - \left( \tilde{u}_R \mathbf{a_u} \tilde{Q} H_u - \tilde{d}_R \mathbf{a_d} \tilde{Q} H_d - \tilde{e}_R \mathbf{a_e} \tilde{L} H_d \right) + \text{h.c.} \\ & - \tilde{Q}^+ \mathbf{m_Q^2} \tilde{Q} - \tilde{L}^+ \mathbf{m_L^2} \tilde{L} - \tilde{u}_R \mathbf{m_u^2} \tilde{u}_R^* - \tilde{d}_R \mathbf{m_d^2} \tilde{d}_R^* - \tilde{e}_R \mathbf{m_e^2} \tilde{e}_R^*\end{aligned}$$

Most general parameterization of SUSY-breaking terms that keep relations between dimensionless couplings unchanged

⇒ no quadratic divergences

$\mathbf{m_i^2, a_j}$ :  $3 \times 3$  matrices in family space

⇒ many new parameters

→ Superpotential of the MSSM

## Particle content of the MSSM:

Superpartners for Standard Model particles:

$$\left[ u, d, c, s, t, b \right]_{L,R} \quad \left[ e, \mu, \tau \right]_{L,R} \quad \left[ \nu_e, \mu, \tau \right]_L \quad \text{Spin } \frac{1}{2}$$

$$\left[ \tilde{u}, \tilde{d}, \tilde{c}, \tilde{s}, \tilde{t}, \tilde{b} \right]_{L,R} \quad \left[ \tilde{e}, \tilde{\mu}, \tilde{\tau} \right]_{L,R} \quad \left[ \tilde{\nu}_e, \mu, \tau \right]_L \quad \text{Spin } 0$$

$$g \quad \underbrace{W^\pm, H^\pm}_{\gamma, Z, H_1^0, H_2^0} \quad \text{Spin 1 / Spin 0}$$

$$\tilde{g} \quad \tilde{\chi}_{1,2}^\pm \quad \tilde{\chi}_{1,2,3,4}^0 \quad \text{Spin } \frac{1}{2}$$

Enlarged Higgs sector:

Two Higgs doublets, physical states:  $h^0, H^0, A^0, H^\pm$

as usual: Breaking of  $SU(2) \times U(1)_Y$  (electroweak symmetry breaking)

⇒ fields with different  $SU(2) \times U(1)_Y$  quantum numbers can mix if they have the same  $SU(3)_c, U(1)_{em}$  quantum numbers

## Squark mixing:

Stop, sbottom mass matrices ( $X_t = A_t - \mu/\tan\beta$ ,  $X_b = A_b - \mu\tan\beta$ ):

$$\mathcal{M}_{\tilde{t}}^2 = \begin{pmatrix} M_{\tilde{t}_L}^2 + m_t^2 + DT_{t_1} & m_t X_t \\ m_t X_t & M_{\tilde{t}_R}^2 + m_t^2 + DT_{t_2} \end{pmatrix} \xrightarrow{\theta_{\tilde{t}}} \begin{pmatrix} m_{\tilde{t}_1}^2 & 0 \\ 0 & m_{\tilde{t}_2}^2 \end{pmatrix}$$

$$\mathcal{M}_{\tilde{b}}^2 = \begin{pmatrix} M_{\tilde{b}_L}^2 + m_b^2 + DT_{b_1} & m_b X_b \\ m_b X_b & M_{\tilde{b}_R}^2 + m_b^2 + DT_{b_2} \end{pmatrix} \xrightarrow{\theta_{\tilde{b}}} \begin{pmatrix} m_{\tilde{b}_1}^2 & 0 \\ 0 & m_{\tilde{b}_2}^2 \end{pmatrix}$$

off-diagonal element prop. to mass of partner quark ( $\tan\beta \equiv v_u/v_d$ )

⇒ mixing important in stop sector (also in sbottom sector for large  $\tan\beta$ )

gauge invariance ⇒  $M_{\tilde{t}_L} = M_{\tilde{b}_L}$  (2)

⇒ relation between  $m_{\tilde{t}_1}, m_{\tilde{t}_2}, \theta_{\tilde{t}}, m_{\tilde{b}_1}, m_{\tilde{b}_2}, \theta_{\tilde{b}}$

Neutralinos and charginos:

Higgsinos and electroweak gauginos mix

charged:

$$\tilde{W}^+, \tilde{h}_u^+ \rightarrow \tilde{\chi}_1^+, \tilde{\chi}_2^+, \quad \tilde{W}^-, \tilde{h}_d^- \rightarrow \tilde{\chi}_1^-, \tilde{\chi}_2^-$$

⇒ charginos: mass eigenstates

mass matrix given in terms of  $M_2$ ,  $\mu$ ,  $\tan\beta$

neutral:

$$\underbrace{\tilde{\gamma}, \tilde{Z}}_{\tilde{W}^0, \tilde{B}^0}, \tilde{h}_u^0, \tilde{h}_d^0 \rightarrow \tilde{\chi}_1^0, \tilde{\chi}_2^0, \tilde{\chi}_3^0, \tilde{\chi}_4^0$$

$$\tilde{W}^0, \tilde{B}^0$$

⇒ neutralinos: mass eigenstates

mass matrix given in terms of  $M_1$ ,  $M_2$ ,  $\mu$ ,  $\tan\beta$

⇒ only one new parameter

⇒ MSSM predicts mass relations between neutralinos and charginos

## 4. Properties of SUSY theories:

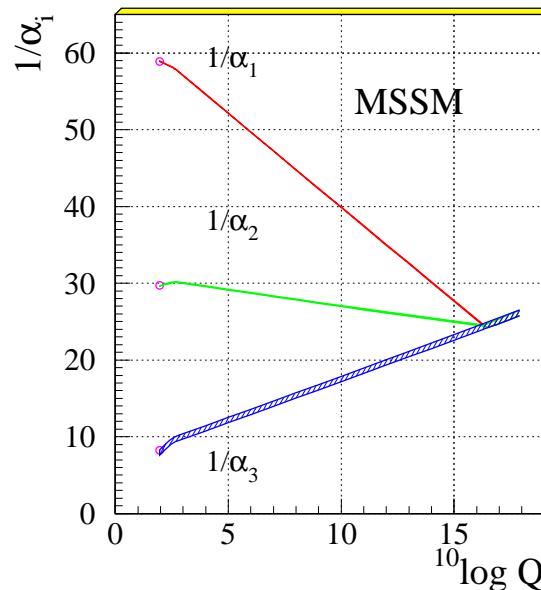
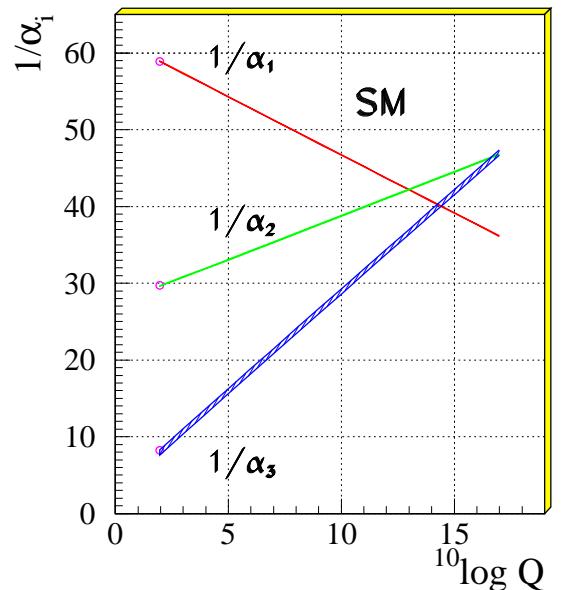
### Property I: coupling constant unification

[RGE: equations that connect parameters at different energy scales]

→ use RGE's to evolve gauge coupling constants from electroweak scale to the GUT scale

$$\alpha_i(Q_{\text{electroweak}}) \rightarrow \alpha_i(Q_{\text{GUT}})$$

#### Unification of the Coupling Constants in the SM and the minimal MSSM



gauge couplings do not meet in the SM

they unify in the MSSM  
although it was not designed for it!

$\Rightarrow M_{\text{SUSY}} \approx 1 \text{ TeV}$

## Property II: the Higgs mechanism comes for free

Higgs mechanism needed to give masses to  $W$  and  $Z$  bosons:

SM: Scalar SU(2) doublet:  $\Phi = \begin{pmatrix} \phi^+ \\ \phi^0 \end{pmatrix}$

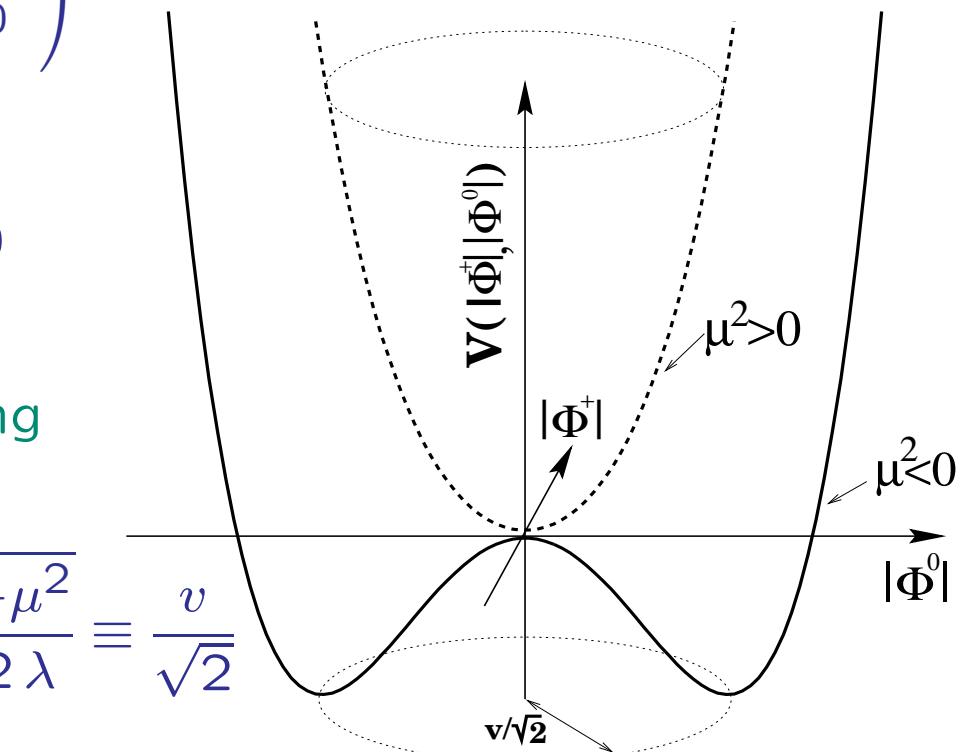
Higgs potential:

$$V(\phi) = \mu^2 |\Phi^\dagger \Phi| + \lambda |\Phi^\dagger \Phi|^2, \quad \lambda > 0$$

$\mu^2 < 0$ : Spontaneous symmetry breaking

minimum of potential at  $|\langle \Phi_0 \rangle| = \sqrt{\frac{-\mu^2}{2\lambda}} \equiv \frac{v}{\sqrt{2}}$

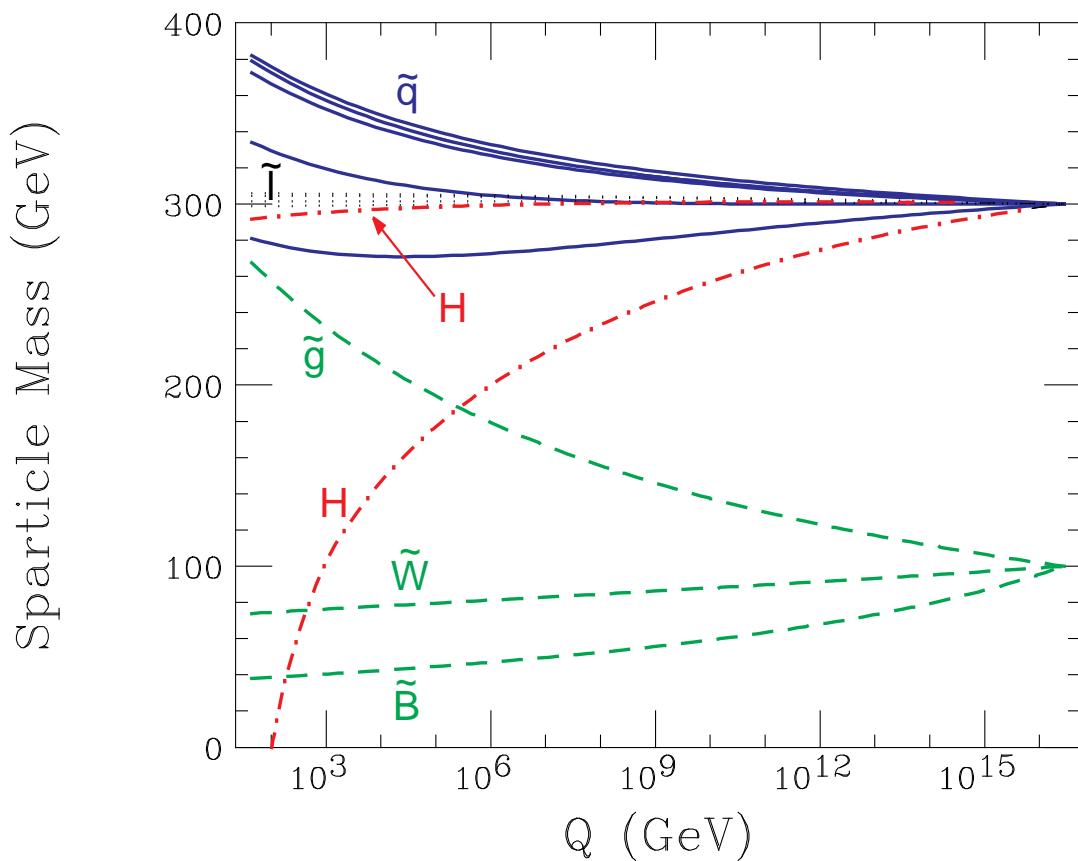
SM: sign of  $\mu$  has to be set by hand



MSSM: negative sign of  $\mu$  comes for free provided that ...

- assume GUT scale (as motivated by coupling constant unification)
- take universal input parameters at the GUT scale (see mSUGRA below)
- run down to the electroweak scale with RGEs

$$M_0 = 300 \text{ GeV}, M_{1/2} = 100 \text{ GeV}, A_0 = 0$$



Exactly one parameter turns negative: the “ $\mu$ ” in the Higgs potential

But this only works if

$$m_t = 150 \dots 200 \text{ GeV}$$

and  $M_{\text{SUSY}} \approx 1 \text{ TeV}$

### Property III: $R$ parity

Most general gauge-invariant and renormalizable superpotential with chiral superfields of the MSSM:

$$\mathcal{V} = \mathcal{V}_{\text{MSSM}} + \underbrace{\frac{1}{2}\lambda^{ijk}L_i L_j E_k + \lambda'^{ijk}L_i Q_j D_k + \mu'^i L_i H_u}_{\text{violate lepton number}} + \underbrace{\frac{1}{2}\lambda''^{ijk}U_i D_j D_k}_{\text{violates baryon number}}$$

If both lepton and baryon number are violated

⇒ rapid proton decay

Minimal choice (MSSM) contains only terms in the Lagrangian with **even** number of SUSY particles

⇒ additional symmetry: “ $R$  parity”

⇒ all SM particles have even  $R$  parity, all SUSY particles have odd  $R$  parity

## Property IV: the LSP

MSSM has further symmetry: “R-parity”

all SM-particles and Higgs bosons: even R-parity,  $P_R = +1$

all superpartners: odd R-parity,  $P_R = -1$

⇒ SUSY particles appear only in pairs, e.g.  $e^+e^- \rightarrow \tilde{\chi}_1^+\tilde{\chi}_1^-$

⇒ lightest SUSY particle (LSP) is stable

(usually the lightest neutralino)

good candidate for Cold Dark Matter

⇒  $M_{\text{SUSY}} \lesssim 1 \text{ TeV}$

LSP neutral, uncolored ⇒ leaves no traces in collider detectors

⇒ Typical SUSY signatures: “missing energy”

## Property V: Relations between SUSY parameters

Symmetry properties of MSSM Lagrangian (SUSY, gauge invariance) give rise to coupling and mass relations

Soft SUSY breaking does not affect SUSY relations between dimensionless couplings

E.g.:

gauge boson–fermion coupling

=

gaugino–fermion–sfermion coupling

for U(1), SU(2), SU(3) gauge groups

In SM: all masses are free input parameters  
(except  $M_W$ - $M_Z$  interdependence)

MSSM:

- Upper bound on mass of lightest  $\mathcal{CP}$ -even Higgs boson
- Relations between neutralino and chargino masses
- Sfermion mass relations, e.g.

$$m_{\tilde{e}_L}^2 = m_{\tilde{\nu}_L}^2 - M_W^2 \cos(2\beta)$$

All relations receive corrections from loop effects

⇒ effects of soft SUSY breaking, electroweak symmetry breaking

⇒ Experimental verification of parameter relations is a crucial test of SUSY!

## Property VI: the mass of the lightest MSSM Higgs boson

Upper bound on  $m_h$  in the MSSM:

“Unconstrained MSSM”:

$M_A$ ,  $\tan\beta$ , 5 parameters in  $\tilde{t}$ – $\tilde{b}$  sector,  $\mu$ ,  $m_{\tilde{g}}$ ,  $M_2$

$$m_h \lesssim 135 \text{ GeV}$$

for  $m_t = 170.9 \pm 1.8 \text{ GeV}$

(including theoretical uncertainties from unknown higher orders)  
⇒ observable at the LHC

Obtained with:

*FeynHiggs*

[S.H., W. Hollik, G. Weiglein '98, '00, '02]

[T. Hahn, S.H., W. Hollik, G. Weiglein '03 – '07]

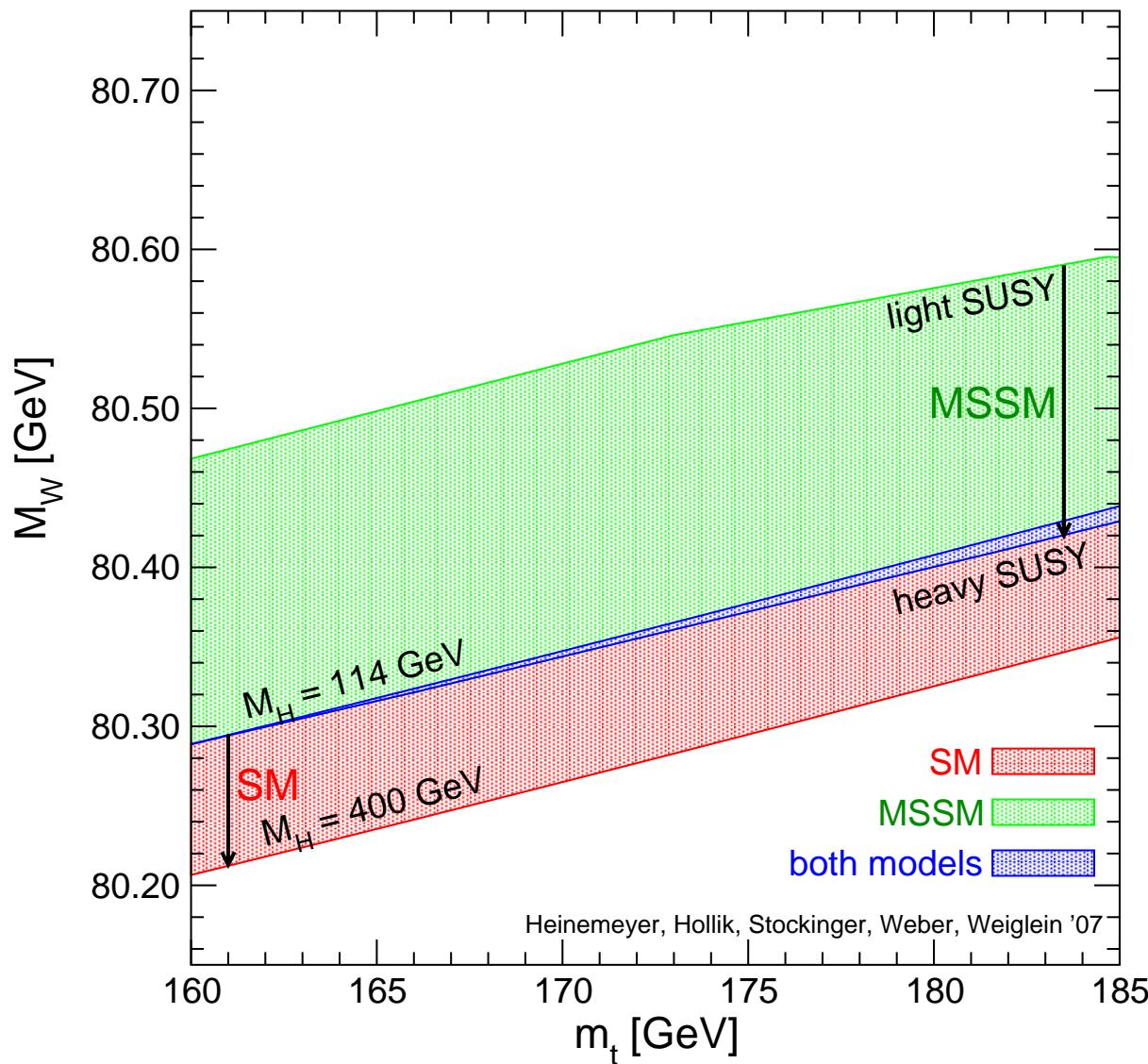
[www.feynhiggs.de](http://www.feynhiggs.de)

→ all Higgs masses, couplings, BRs (easy to link, easy to use :-)

## Property VII: the mass of the $W$ boson

Prediction for  $M_W$  in the **SM** and the **MSSM** :

[*S.H., W. Hollik, D. Stockinger, A.M. Weber, G. Weiglein '06*]



**MSSM band:**

scan over

SUSY masses

**overlap:**

SM is MSSM-like

MSSM is SM-like

**SM band:**

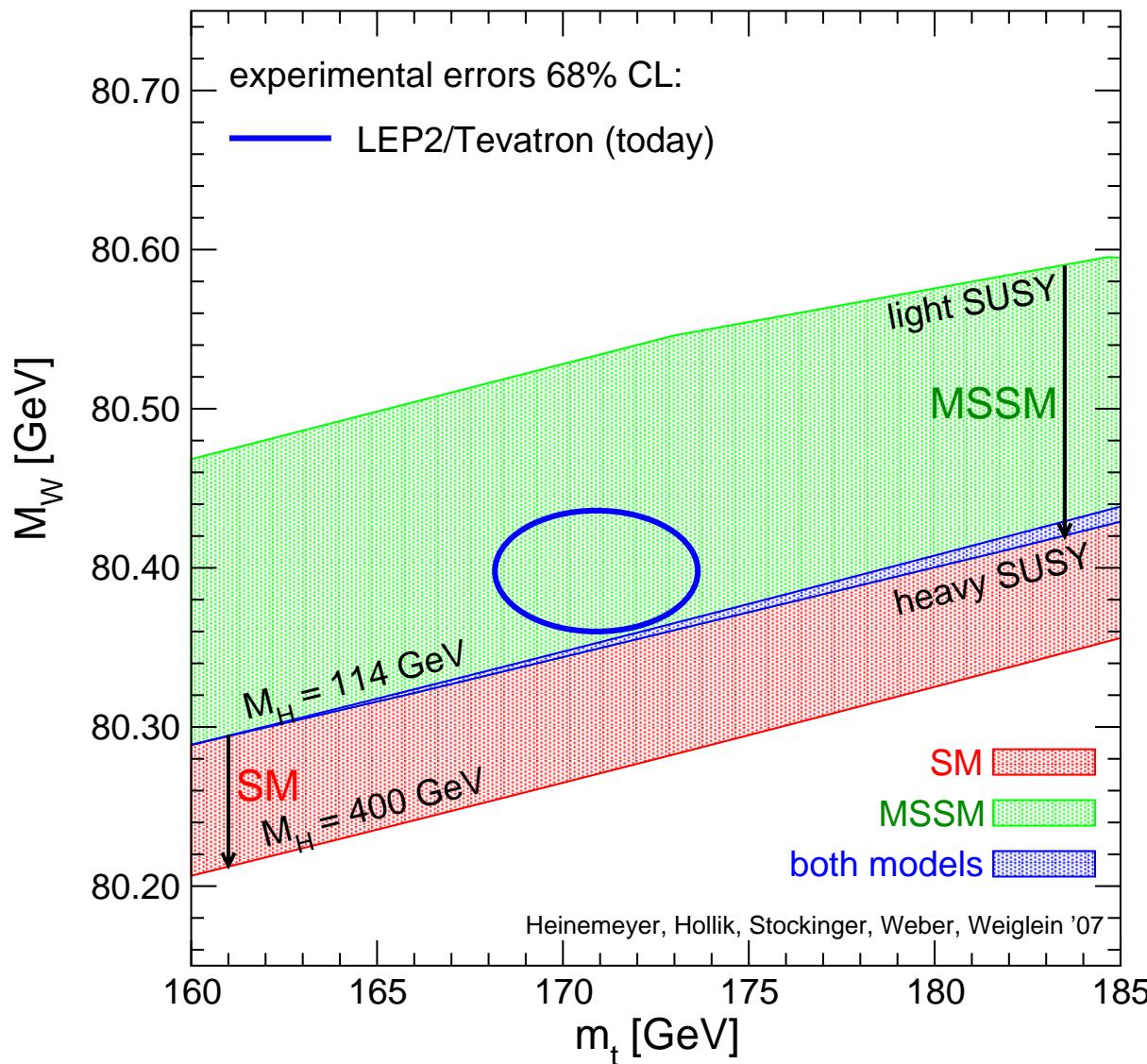
variation of  $M_H^{\text{SM}}$

## Property VII: $M_W$

$$M_W = 80.398 \pm 0.025 \text{ GeV}, m_t = 170.9 \pm 1.8 \text{ GeV}$$

Prediction for  $M_W$  in the SM and the MSSM :

[S.H., W. Hollik, D. Stockinger, A.M. Weber, G. Weiglein '06]



MSSM band:

scan over  
SUSY masses

overlap:

SM is MSSM-like  
MSSM is SM-like

SM band:

variation of  $M_H^{\text{SM}}$